

(2)

- (e) What do you mean by renormalization? 2
- (f) Show that $\gamma_\mu \gamma^\nu \gamma^\mu = -2\gamma^\nu$. 2
- (g) Write down the Feynman function for scalar field. 2
- (h) What do you mean by normal order product of operators and fields? 2
- (i) What is the charge of the particles associated with real and complex scalar field? 2
- (j) State Wick's theorem. 2
2. (a) Derive the Klein-Gordon equation for a relativistic particle with zero spin. Discuss the probability density and continuity equation. 8
- (b) Discuss the drawbacks of Klein-Gordon equation. 2
3. (a) Solve the Dirac equation for a free particle in motion. 8
- (b) Discuss the properties of the Dirac matrices. 2

(3)

4. (a) What are bilinear covariants? Show how the vector and axial vector transform under proper orthochronous Lorentz transformation and space inversion. 7
- (b) Show that the particle described by the Dirac equation corresponds to a spin $1/2$ particle. 3
5. (a) Discuss what happens to the Lagrange equation and quantization conditions on going from a discrete to a continuous system. 3
- (b) State Noether's theorem. Find the conserved quantities arising out of rotational invariance. 7
6. (a) Quantize the complex Klein-Gordon field and find the momentum and charge of the field. 7
- (b) Discuss the time-ordered product of operators. 3
7. (a) Quantize the Dirac field and find the momentum, energy and charge of the field. 7
- (b) Discuss the photon propagator for real Dirac field. 3